

Gemini/Phoenix H-band analysis of the globular cluster AL 3 [★]

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ABSTRACT

Context. The globular cluster AL 3 is old and located in the inner bulge. Three individual stars were observed with the Phoenix spectrograph at the Gemini South telescope. The wavelength region contains prominent lines of CN, OH, and CO, allowing the derivation of C, N, and O abundances of cool stars.

Aims. We aim to derive C, N, O abundances of three stars in the bulge globular cluster AL 3, and additionally in stars of NGC 6558 and HP 1. The spectra of AL 3 allows us to derive the cluster's radial velocity.

Methods. For AL 3, we applied a new code to analyse its colour-magnitude diagram. Synthetic spectra were computed and compared to observed spectra for the three clusters.

Results. We present a detailed identification of lines in the spectral region centred at 15555 Å, covering the wavelength range 15525-15590 Å. C, N, and O abundances are tentatively derived for the sample stars.

Key words. Stars: Abundances, Atmospheres – Galaxy Bulge – Globular clusters: individual: AL 3, NGC 6558, HP 1

1. Introduction

The globular clusters AL 3, NGC 6558, and HP 1 share the characteristics of having a metallicity of $[Fe/H] \sim -1.0$ and of being located in the Galactic bulge. They are old and could represent the earliest stellar populations in the Galaxy (Ortolani et al. 2006; Barbuy et al. 2018a; Kerber et al. 2019).

The star cluster AL 3 was discovered by Andrews & Lindsay (1967) and was also cataloged as BH 261 by van den Bergh & Hagen (1975), reported as a faint open cluster. It is reported in the ESO/Uppsala catalogue (Lauberts 1982) as ESO 456-SC78. Ortolani et al. (2006) showed that the star cluster shows B, V, I colour-magnitude diagrams (CMD) typical of a globular cluster. It is centred at J2000 $\alpha = 18^{\text{h}}14^{\text{m}}06.6^{\text{s}}$, $\delta = -28^{\circ}38'06''$, with Galactic coordinates $l = 3.36^{\circ}$, $b = -5.27^{\circ}$, and located at 6:25 and 2 kpc from the Galactic centre, hence in the inner bulge volume. The cluster has a depleted red giant branch (RGB), similarly to low-mass Palomar clusters, indicating it to have been stripped along its lifetime. This cluster has not been further observed so far.

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* Observations collected at the Gemini Observatory, Proposals GS-2006A-C9 and GS-2008A-Q-23-5, and at the European Southern Observatory (ESO), Proposal 64L-0212(A).

The NGC 6558 cluster is located in a window, identified by Blanco (1988), with equatorial coordinates (J2000) $\alpha = 18^{\text{h}}10^{\text{m}}18.4^{\text{s}}$, $\delta = -31^{\circ}45'49''$ and Galactic coordinates $l = 0.201^{\circ}$, $b = -6.025^{\circ}$. It was analysed in terms of CMD by Rich et al. (1998). Rossi et al. (2015) obtained a proper-motion-cleaned CMD and presented a proper motion analysis, from which a study of its orbits was given in Pérez-Villegas et al. (2018, 2020).

The globular cluster Cl Haute-Provence 1 or HP 1, also designated BH 229 and ESO 455-SC11, was discovered by Dufay et al. (1954). It is located at J2000 $\alpha = 17^{\text{h}}31^{\text{m}}05.2^{\text{s}}$, $\delta = -29^{\circ}58'54''$, with Galactic coordinates $l = 357.42^{\circ}$, $b = 2.12^{\circ}$.

In the present work, we studied individual stars of these clusters in a limited region of the spectrum in the H-band corresponding to the wavelength region of the Phoenix spectrograph at the Gemini South telescope, centred at 15555 Å, and covering 15520-15590 Å, with a high spectral resolution of $R \sim 75,000$. This region was chosen for containing prominent lines of CN, CO, and OH.

In Sect. 2, we examine the list of atomic and molecular lines in the region. In Sect. 3, the observations are described. In Sect. 4, the CMD is analysed. In Sect. 5, the stellar parameters are given. In Sect. 6, the C, N, O abundances are derived. Conclusions are drawn in Sect. 7.

2. Spectroscopy in the H-band: Atomic and molecular lines

The H-band will be intensely observed in the near future, given the new instruments placing emphasis on the near-infrared region, such as the James Webb Space Telescope (JWST), and new spectrographs on ground-based telescopes such as MOONS@VLT (presently CRIRES@VLT is available) and MOSAIC@ELT. The project APOGEE (Apache Point Observatory Galactic Evolution Experiment), with observations at a resolution of $R \sim 22,000$ carried out at the 2.5-metre Sloan Foundation Telescope at the Apache Point Observatory in New Mexico (APOGEE-2N), and the 2.5-metre du Pont Telescope at Las Campanas Observatory in Chile (APOGEE-2S), as described in Majewski et al. (2017) has shown the power of the H-band.

Given the short wavelength range covering only 70 \AA of the Phoenix spectrograph, we faced the challenge of identifying the lines in moderately metal-poor stars of the Galactic bulge, for which only a few lines are available. Because the available lamps did not include lines in this region, and experience proved that sky lines yielded a better wavelength calibration, and given the short wavelength range, it is not straightforward to identify the lines.

For this reason, we proceeded to a line identification, in the spectra of the reference stars Arcturus and μ Leo, and created a shortened version of a line list, containing only detectable lines.

Meléndez & Barbuy (1999, hereafter MB99) worked on a list of atomic lines in the J and H bands. The list of lines mostly corresponded to the detectable lines. That previous line list needed to be largely completed. Upon checking the lines detectable in the wavelength range $15520\text{--}16000 \text{ \AA}$, this was done by verifying the line lists from APOGEE (Shetrone et al. 2015) and VALD (Piskunov et al. 1995, Ryabchikova et al. 2015). We note that astrophysical oscillator log gf strengths were applied to the APOGEE line list, and these should be suitable for abundance derivation. Through a line-by-line check of its detectability in the Arcturus spectrum, we identified lines of Mg I, Si I, Ca I, Ti I, Mn I, and Ni I, and we were not able to find detectable lines from the species C I, O I, Sc I, V I, Cr I, Co I, Cu I, Y I, and Y II. The spectra computed including all lines of all these elements are entirely equivalent to the one computed with the shortened line list, therefore to ensure practicality when identifying which lines really contribute to a feature, we created a table containing the detectable lines only. In this table, available upon request, we report the oscillator strengths from MB99, APOGEE, VALD, and adopted values, where in order of preference we adopted NIST and MB99.

Molecular electronic transition lines of CN $A^2\Pi\text{--}X^2\Sigma$, and vibration-rotation CO $X^1\Sigma^+\text{--}X^1\Sigma^+$, OH $X^2\Pi\text{--}X^2\Pi$ lines were included in the synthetic spectra calculations. The line lists for CN were made available by S. P. Davis, the CO line lists were adopted from Goorvitch (1994), and the OH line list was made available by S. P. Davis and A. Goldman (Goldman et al. 1998). For more details on CN, CO, and OH molecular lines, we refer the reader to Meléndez & Barbuy (1999), Meléndez et al. (2001), and Meléndez et al. (2002). TiO ϕ -system $b^1\Pi\text{--}d^1\Sigma$ lines are also present in the region. The line list by Jorgensen (1994) is included in the calculations as described in Schiavon & Barbuy (1999) and Barbuy et al. (2018a). The adopted dissociation potential of OH is 4.392 eV , $D_0 = 11.092 \text{ eV}$ for CO and $D_0 = 7.65 \text{ eV}$ for CN (Huber & Herzberg 1979). The PFANT code employed here for calculations of synthetic spectra is described in Barbuy et al.

Table 1. Log book of observations. Proposals GS-2006A-C9 on 15/16/07/2006, and GS-2008A-Q-23 on 10/04/2008 and 22/05/2008

Object	Date	LST h:m	Exp. (m)	Seeing (")
NGC 6558-11	15-07-2006	22:00	2x25	0.6
NGC 6558-64	16-07-2006	14:48	3x30	0.7
NGC 6558-11	16-07-2006	16:33	2x20	0.5
NGC 6558-42	16-07-2006	19:13	2x30	0.7
NGC 6558-97	16-07-2006	20:25	3x20	0.6
NGC 6558-73	16-07-2006	21:38	2x30	0.9
HP 1-4	15-07-2006	13:42	3x30	0.6
HP 1-6	15-07-2006	20:12	3x30	0.6
HP 1-5	16-07-2006	13:03	3x30	0.8
HP 1-3	16-07-2006	18:02	2x30	0.6
AL 3-3	10-04-2008	15:58	4x15	—
AL 3-6	22-05-2008	15:09	4x15	—
AL 3-7	22-05-2008	16:21	4x15	—

(2018b), and it is available together with the atomic and molecular line lists.¹

We identified the lines in the reference stars Arcturus and μ Leo. For the reference star Arcturus, the spectrum atlas from Hinkle et al. (1995) is used, and for the metal-rich reference giant star μ Leo, APOGEE spectra are used, and their studies are presented elsewhere.

The adopted stellar parameters for Arcturus and μ Leo are from Meléndez et al. (2003) and Lecureur et al. (2007), and they are reported in Sect. 5.

3. Observations

The spectra of red giant stars of the bulge globular clusters NGC 6558, AL 3, and HP 1 were observed with the Phoenix spectrograph installed on the 8m Gemini South telescope. The program was tri-national from Brazil (PI: B. Barbuy), Chile (PI: M. Zoccali), and Australia (PI: J. Meléndez).

The final suitable spectra include three stars of AL 3, two stars of NGC 6558, and one star of HP 1, centred at $1.555 \mu\text{m}$ in the H band. Another three stars in NGC 6558, and three in HP 1 were also observed; however, these showed a low Signal-to-Noise (S/N), due to clouds or high airmass. The log of observations is provided in Table 1.

This is the first spectroscopic work on AL 3, except for Gaia data (Gaia Collaboration 2020). In Fig. 1, a 3 min B exposure of AL 3 is shown for a field extraction of $3.3' \times 3.3'$ (510×510 pixels). The sample stars of AL 3 are identified in the chart. Charts and identifications of the observed stars in NGC 6558 and HP 1 are given in Barbuy et al. (2009, 2018) and Barbuy et al. (2006, 2016), respectively.

3.1. Gaia cross-check

In order to verify the corresponding membership probability of observed stars in AL 3, we performed the cross-match with Gaia Early Data Release 3 (EDR3; Gaia Collaboration 2020). We selected stars within $20'$ from the cluster centre and used the renormalised unit weight error (RUWE) ≤ 2.4 to ensure the kinematics precision and the minimum match separation.

¹ <http://trevisanj.github.io/PFANT>

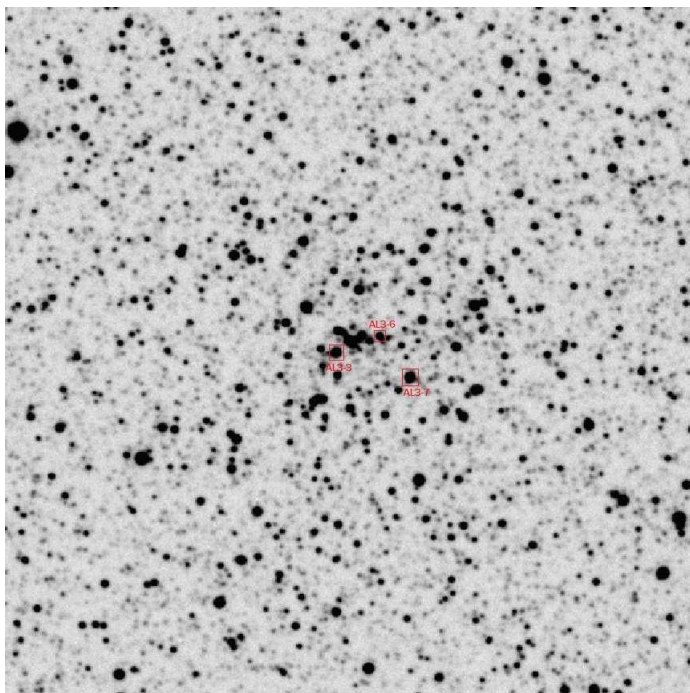


Fig. 1. AL 3: 3 min B image with the three sample stars identified. Extraction of $3' \times 3'$. North is up and east is left.

Having the high-precision EDR3 proper motions ($\mu_\alpha^* = \mu_\alpha \cos \delta$ and μ_δ), we obtain the mean proper motions for the cluster of $\mu_\alpha^* = 3.59 \pm 0.03 \text{ mas yr}^{-1}$ and $\mu_\delta = -3.54 \pm 0.04 \text{ mas yr}^{-1}$. These values are compatible with those given in Baumgardt et al. (2019). We also computed the Gaussian membership probability distribution of AL 3. We found that the stars AL3-6 and AL3-7 have membership probabilities of 100%. Finally, the star AL3-3 has a relatively low membership probability of $\sim 60\%$, but still, it could be considered a member. Therefore, all three observed stars are probable members of AL 3. Table 2 provides the Gaia EDR3 cross-match and the membership probabilities.

3.2. Radial velocity of AL 3

We were able to derive radial velocities for the sample stars. We used the low S/N individual observations of each star ($S/N \sim 10.0$) combined to increase the signal-to-noise to $S/N \sim 18.0$, and $S/N \sim 22.0$ for AL3-3 and AL3-7, respectively. Due to the stacking process, the most prominent features identified are FeI 15,534.26, OH 15,542.10, TiI 15,543.758, TiO/NiI 15,55.25 blend, CN 15,555.25, and FeI 15,591.49. We also used the OH sky lines, as listed in Table 2 by Meléndez et al. (2003). These features were used for AL3-3, giving a radial velocity of $-67.65 \pm 3.65 \text{ km s}^{-1}$. In the combined spectrum of AL3-7, the same features result in a radial velocity of $-68.93 \pm 4.83 \text{ km s}^{-1}$. The corresponding heliocentric velocities of -57.29 km s^{-1} and -58.57 km s^{-1} lead to a final mean heliocentric velocity of $-57.93 \text{ km s}^{-1} \pm 4.28$ for AL 3. Figures 2 and 3 show the line identification and radial velocity derivation.

The star AL3-6 shows a very noisy spectrum, and we verified that it was observed under a high airmass of over 1.3, which also explains that it is plagued with telluric features. For AL3-6, we obtained a different heliocentric radial velocity, as shown in Fig. 4, of $-29.57 \pm 5.85 \text{ km s}^{-1}$, compatible with the value given by Baumgardt et al. (2019) of $-29.38 \pm 0.60 \text{ km s}^{-1}$.

The derived radial velocity is of crucial importance for the computation of the cluster's orbits - see Sect. 5. However, we obtained two different figures: $v_r^{\text{hel}} = -57.93$ and -29.57 km s^{-1} . In Fig. 4, we show the spectrum of AL3-6 compared with that of AL3-7. Therefore, we obtained two different radial velocities for AL 3, and consequently we considered both of them for the calculation of orbits. Since we had already computed the orbits for the lower value (from Baumgardt et al. 2019), we show the orbits for the higher value here. Clearly, new observations of these stars in a more extended wavelength range and with a higher S/N would be of great interest.

4. Colour-magnitude diagram of AL 3

Ortolani et al. (2006) presented B , V , and Cousins I images of AL 3, observed on 2000 March 6 using the 1.54m Danish telescope at the European Southern Observatory (ESO) at La Silla. They derived a reddening of $E(B-V) = 0.36 \pm 0.03$ and a distance of $6.0 \pm 0.5 \text{ kpc}$, based on the magnitude of the horizontal branch (HB) of AL 3, and suggested a metallicity of $[\text{Fe}/\text{H}] = -1.3 \pm 0.3$ from a comparison of the CMD with the mean locus of the cluster M5.

Rossi et al. (2015) described the observations with EFOSC at the NTT (ESO), La Silla in May 2012. They reported a distance of $\sim 6.5 \text{ kpc}$, in agreement with Harris (1996, 2010 edition). Pérez-Villegas et al. (2020) adopted both distances of 6.0 and 6.5 kpc and the radial velocity from Baumgardt et al. (2019) for the calculation of orbits.

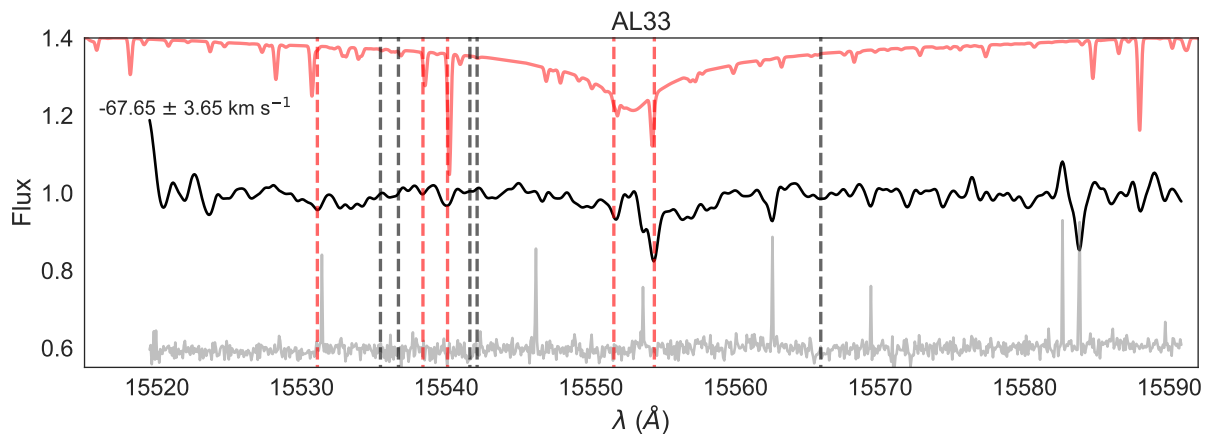
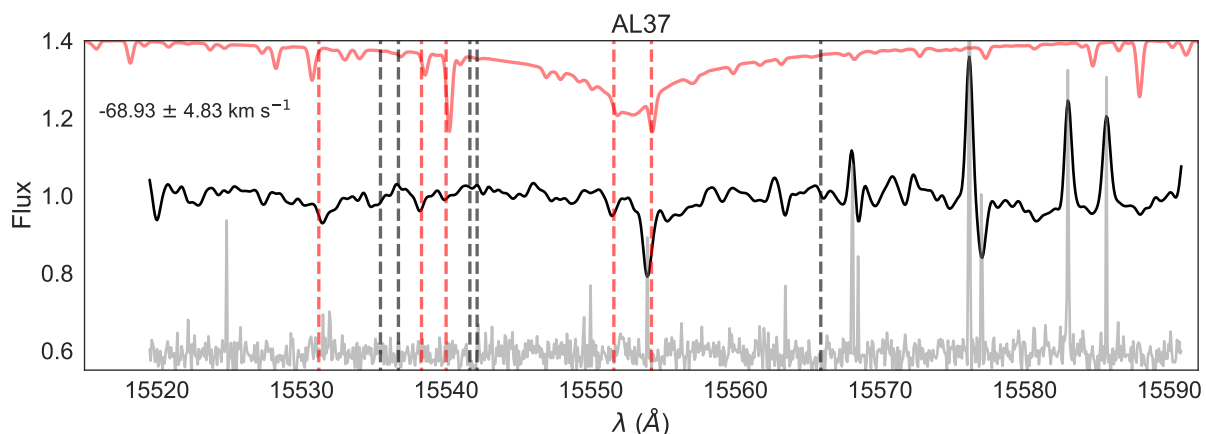
We carried out the isochrone fitting using the SIRIUS code (Souza et al. 2020) on the same AL 3 data presented in Ortolani et al. (2006). The metallicity was limited by using a Gaussian prior with the value of Ortolani et al. (2006). We adopted the Dartmouth Stellar Evolution Database (DSED - Dotter et al. 2008), with $[\alpha/\text{Fe}] = 0.4$ and primordial helium. The asymptotic giant branch (AGB) is also shown, based on BaSTI isochrones (Pietrinferni et al. 2006), since they are not available in DSED. The result is in very good agreement with results from Ortolani et al. (2006) within $1 - \sigma$. We obtain a reddening of $E(B-V) = 0.38 \pm 0.04$, a distance of $d_\odot = 6.0 \pm 0.6 \text{ kpc}$, and a metallicity of $[\text{Fe}/\text{H}] = -1.34 \pm 0.18$. Our age determination indicates an old age of $13.4_{-1.2}^{+1.0} \text{ Gyr}$, indicating that AL 3 is another relic fossil. It is important to stress that our distance of 6.0 kpc is also in agreement, within $1 - \sigma$, with the value of 6.5 kpc from Harris (1996, 2010), Rossi et al. (2015), and Baumgardt et al. (2019).

Finally, we note that the dispersion of the data could be due to differential reddening, together with contamination and blends. The reddening of AL 3 is relatively high, and the differential reddening is certainly an issue, as it is in other bulge globular clusters with similar reddening. We expect an amount of about 20% of differential reddening. In principle it can be corrected, but the standard procedures for differential reddening correction in this cluster cannot be applied due to the few bona fide reference stars in the CMDs.

Figure 5 shows the solution of isochrone fitting. The solid blue line represents the median solution, while the shaded regions indicate the solutions within $1 - \sigma$. The red stars are the three sample stars. Finally, Figure A.1 exhibits the corner plots showing the (anti)correlations between the parameters.

Table 2. Gaia magnitudes, proper motions and membership probability.

Star	α (J2000) deg	δ (J2000) deg	G mag	G_{RP} mag	μ_{α}^* mas yr $^{-1}$	μ_{δ} mas yr $^{-1}$	Memb %
AL3-3	273.5288067	-28.6357960	14.186 ± 0.003	13.323 ± 0.004	3.78 ± 0.09	-4.04 ± 0.07	59
AL3-6	273.5247404	-28.6346067	15.228 ± 0.003	14.303 ± 0.011	3.56 ± 0.06	-3.64 ± 0.04	100
AL3-7	273.5220767	-28.6380356	13.924 ± 0.003	13.062 ± 0.005	3.58 ± 0.03	-3.48 ± 0.03	100


Fig. 2. AL 3-3: Radial velocity derivation. The solid black line is the observed spectrum, the solid grey line is the noise spectrum, the solid red line is the synthetic spectrum, the dashed red lines are those used to derive the radial velocity, and the dashed black lines are the OH sky lines.

Fig. 3. AL 3-7: Radial velocity derivation. The solid black line is the observed spectrum, the solid grey line is the noise spectrum, the solid red line is the synthetic spectrum, the dashed red lines are those used to derive the radial velocity, and the dashed black lines are the OH sky lines.

5. Stellar parameters

5.1. NGC 6558 and HP 1

Individual stars of NGC 6558 were analysed with high-resolution spectroscopy by Barbuy et al. (2007, 2018b) and with moderate-resolution spectroscopy by Dias et al. (2015). The stars NGC6558-42 and NGC6558-64 are studied here.

Similar studies of HP 1 were carried out in Barbuy et al. (2006, 2016) and Dias et al. (2016). In the 2006 article, the bright red giants were labelled with numbers 1 to 6, for the purpose of identifying them in the cluster chart. In 2016, we adopted the identification numbers corresponding to the photometric reductions relative to observations obtained at the New Technology

Telescope (NTT) at ESO, in 1994, as described in Ortolani et al. (1997). HP1-4 and HP1-5 are stars 2115 and 2939 in Barbuy et al. (2016). HP1-2 is the same as in Barbuy et al. (2006). In our study, we only analysed HP1-5.

5.2. AL 3

The magnitudes and colours as follows are indicated in Table 3: B, V from Ortolani et al. (2006), V, I from Rossi et al. (2015),

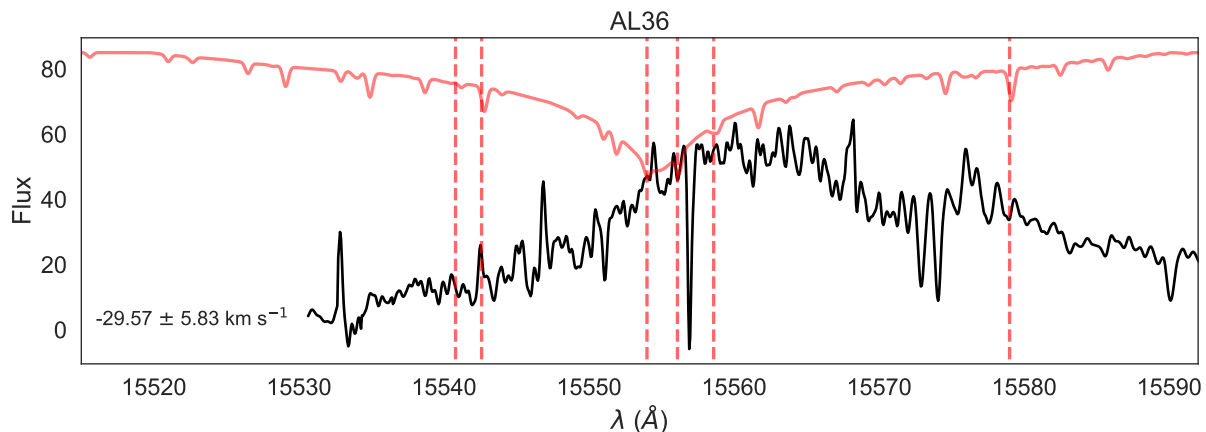


Fig. 4. AL 3-6: Radial velocity derivation. The solid black line is the observed spectrum, the solid grey line is the spectrum of star AL3-7, the dashed red lines are those used to derive the radial velocity, and the dashed black lines are the OH sky lines.

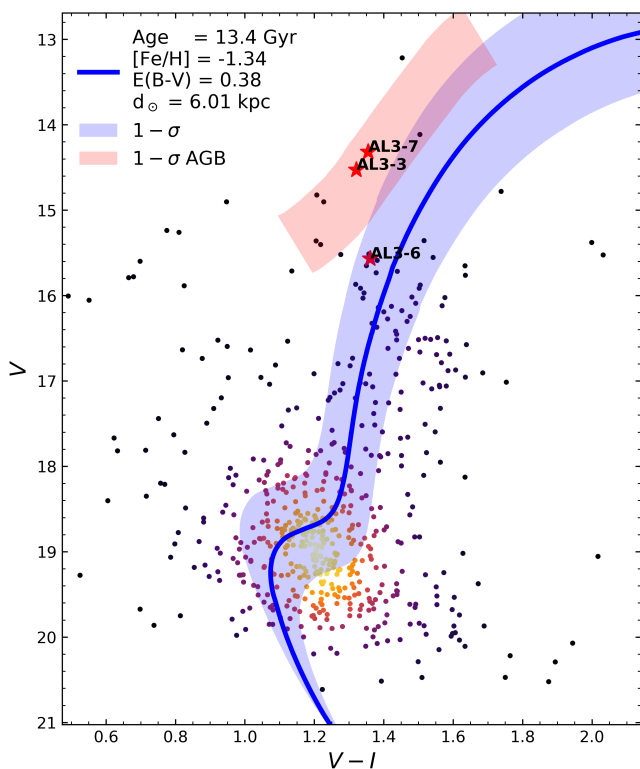


Fig. 5. AL 3 V vs. $V - I$ CMD. The black dots are the stars within 120 pixel from the cluster centre (see Ortolani et al. 2006). The red stars are the observed stars of the present work. The solid blue line represents the median solution of the isochrone fitting, while the blue region reveals the solutions within $1 - \sigma$.

JHK from the 2MASS catalogue (Skrutskie et al. 2006),² and JHK from the VVV survey (Saito et al. 2012).³

Effective temperatures were initially derived from $B - V$, $V - I$, $V - K$, and $J - K$ using the colour-temperature calibrations of Alonso et al. (1999). V,I Cousins were transformed to V,I Johnson using $(V - I)_C = 0.778(V - I)_J$ (Bessell 1979).

² <http://ipac.caltech.edu/2mass/releases/allsky/>;
<https://irsa.iapc.caltech.edu>

³ horus.roe.ac.uk/vsa

The J , H , K_S magnitudes and colours were transformed from the 2MASS system to California Institute of Technology (CIT), and from this to Telescopio Carlos Sánchez (TCS), using the relations established by Carpenter (2001) and Alonso et al. (1998). The conversion of JHK VVV colours to the JHK 2MASS system was done using relations by Soto et al. (2013).

The temperatures resulting from photometry are of the order of 5000 K for the three stars. These temperatures, however, are not compatible with another indicator, which is the Hydrogen Brackett 16 line, centred at 15556.457 Å. A fit of this line for both AL 3 stars was carried out iteratively, after deriving their CNO abundances. The resulting temperatures, adopted in the following analysis, are 4250 K and 4500 K for AL3-3 and AL3-7, respectively. The fits to the hydrogen line are shown in Figure 6. For AL3-6, the low quality of the spectrum does not allow the fit of the hydrogen line, in particular due to strong telluric absorptions in the region. It appears to be cooler and compatible with 4150 K. This incompatibility between photometric and hydrogen-derived temperatures is a main source of uncertainty in the present study.

To derive the gravity, we used the PARSEC isochrones (Bresnan et al. 2012).⁴ To inspect the isochrones, we adopted a metallicity of $[\text{Fe}/\text{H}] = -1.0$, or overall metallicity $Z = 0.00152$ (10 times below solar), and an age of 12 Gyr. Assuming a reddening of $E(B - V) = 0.36$ (Ortolani et al. 2006, and present results), leading to $E(V - I) = 0.478$ and $A_V = 1.12$, we transformed the apparent magnitudes to absolute magnitudes, as well as the colours ($V - I_{\text{corr}} = V - I - E(V - I)$), and we identified the correspondence of the observed stars to the theoretical isochrone.

The metallicity resulting from the CMD fitting is $[\text{Fe}/\text{H}] = -1.34$, which was imposed as a prior. We inspected individual lines of Fe in the AL3-3 spectrum and the fits are more compatible with $[\text{Fe}/\text{H}] = -1.0$. There is also the evidence from other similar bulge globular clusters such as NGC 6558, NGC 6522, HP 1, and Terzan 9, which are found to have $[\text{Fe}/\text{H}] \sim -1.0$ from high-resolution spectroscopy. Bica (2016) showed that there is a peak in metallicity at $[\text{Fe}/\text{H}] \sim -1.0$ in the bulge, which we also adopted for AL 3. An isochrone fitting with this higher metallicity was tried, but appeared difficult to converge. This is a second source of uncertainty of the present study. Final adopted stellar parameters for program stars, and of the reference stars Arcturus

⁴ <http://stev.oapd.inaf.it/cgi-bin/cmd>

(Meléndez et al. 2003) and μ Leo (Lecureur et al. 2007), are reported in Table 4.

6. CNO abundances

The atmospheric models were interpolated in the grid of models by Gustafsson et al. (2008). The synthetic spectra were computed employing the PFANT code described in Barbuy et al. (2018b). In order to derive the C, N, O abundances, we fitted the CN, OH, and CO lines iteratively.

6.1. The cool red giant N6558-42

The cool red giant, NGC6558-42, shows strong lines and is a typical red giant. For this reason, we show the fits to the spectrum of this star in detail in Figures 8 and 9.

The star NGC6558-64 instead, which would have an effective temperature of 4850 K according to the analysis from optical spectra by Barbuy et al. (2018b), could be as hot as 5500 K. This is seen from the profile of its Hydrogen Brackett 16 line; however, this should be taken with caution due to defects in the observed spectrum. For this reason, we could not converge on CNO abundances for this star.

6.2. AL-3 and HP 1

There is a clear contrast between the spectra of HP1-5, AL3-3, and AL3-7, that have shallow lines, and AL3-6 and NGC6558-42, that show strong lines. Whereas NGC6558-42 is a typical red giant, the stars AL3-3, AL3-7, and HP1-5 show weak molecular lines. From the location of stars AL3-3 and AL3-7 in the CMD of Fig. 5, they should be AGB stars. In Fig. 10, we show the observed spectrum in the selected wavelength regions containing CN, OH lines, and the CO bandhead at 15578 Å for stars AL3-3, AL3-7, and HP1-5. The molecular lines are very shallow, due to a combination of warm temperatures and low metallicities. Clearly, the CNO abundances derived for these stars are less reliable than for the cool star NGC6558-F42. Their CNO abundances are compatible with being close to solar, but given the shallowness of the lines, it is clear that the molecular lines are not reliable for abundance measurements.

AL3-6 instead shows very strong CNO lines. Figure 7 indicates that $[C/Fe]=+0.7$, 0.8 , $[N/Fe]=+1.0$, $[O/Fe]=+0.8$ for this star. We show two different renormalisations to illustrate the difficulty in analysing this spectrum. Additionally, the computations with two different carbon abundances illustrate the extreme sensitivity of the lines. Clearly, however, there is an urgent need to observe this star in the optical and/or in a more extended wavelength region in the H-band to obtain firm conclusions on the CNO abundances of AL 3.

6.3. Errors

The main uncertainty in the derivation of CNO abundances in AL 3 stems from the effective temperatures. Adopting a colour excess $E(B-V)=0.36$ the photometric magnitudes results in temperatures of ~ 5000 K. In order to be compatible with the wings of hydrogen lines, we would have to adopt $E(B-V)=0.2$, but the present fit of the CMD confirms the high reddening value.

Hydrogen wings that we adopted are a very good temperature indicator, and the temperatures can be roughly derived for the two stars showing the line, whereas for the cooler star AL3-6, the H line is not strong, indicating that it is cooler than the other

two stars. For this star, we adopted $T_{\text{eff}} = 4150$ K, compatible with its almost absent hydrogen-profile and a temperature compatible with its location in the RGB. With this temperature, we obtained high CNO values and could not converge with lower values. We note that the CN, CO, and OH dissociation equilibrium interplay gives a strong constraint on the result, but at the same time, these are very sensitive to abundance variations. We adopted effective temperature errors of ± 250 K for AL3-6, and ± 150 K for AL3-3 and AL3-7, errors of ± 0.8 for the gravity, and ± 0.3 for metallicity.

6.4. Orbits of AL 3

In order to investigate whether AL 3 belongs to the bulge, thick disc, or halo, given its solar CNO abundances, we carried out the calculations of orbits for the cluster. We employed a Galactic model that includes an exponential disc made by the superposition of three Miyamoto-Nagai potentials (Smith et al. 2015), a dark matter halo with a Navarro-Frenk-White (NFW) density profile (Navarro, Frenk & White 1997), and a triaxial Ferrers bar. The total mass of the bar is $1.2 \times 10^{10} M_{\odot}$, an angle of 25° with the Sun-major axis of the bar, and a major axis extension of 3.5 kpc. We assumed three pattern speeds of the bar $\Omega_b = 40, 45, \text{ and } 50 \text{ km s}^{-1} \text{ kpc}^{-1}$. We kept the same bar extension, even though we changed the bar pattern speed. Our Galactic model has a circular velocity $V_0 = 241 \text{ km s}^{-1}$ at $R_0 = 8.2 \text{ kpc}$ (Bland-Hawthorn & Gerhard 2016; which is also compatible with the Gravity Collaboration et al. (2019)), and we assumed a peculiar motion of the Sun with respect to the local circular orbit of $(U, V, W)_{\odot} = (11.1, 12.24, 7.25) \text{ km s}^{-1}$ (Schönrich, Binney & Dehnen 2010).

To take into account the effects of the observational uncertainties associated with the cluster's parameters, we generated a set of 1000 initial conditions using a Monte Carlo method considering the errors of distance, heliocentric radial velocity, and absolute proper motion components. With such initial conditions, we integrated the orbits forward for 10 Gyr using the NIGO tool (Rossi 2015).

In Fig. 11, we show the probability density map of the orbits of AL 3 in the $x-y$ and $R-z$ projections co-rotating with the bar, using the two adopted distances, 6.0 kpc (Ortolani et al. 2006) and 6.5 kpc (Baumgardt et al. 2019). The yellow colour displays the space region that the orbits of AL 3 cross more frequently. The black curves are the orbits using the central values of the observational parameters. In Figure 12, we show histograms relating to the number of probable orbits as a function of pericentric distance (r_{min}), apocentric distance (r_{max}), maximum height above the plane ($|Z|_{\text{max}}$), and eccentricity (e). In Table 5, we give the median values of the orbital parameters, and the errors provided in each column are derived considering the 16th and 84th percentiles of the distribution. The orbital parameters are similar for the three pattern speeds. From the apocentric distance, we can see that AL 3 is mostly confined within ~ 4 kpc, and it has a high probability to belong to the bulge component ($\sim 88\%$) when the adopted distance is 6.5 kpc. However, a significant fraction of orbits can reach apocentric distances up to ~ 6 kpc, indicating that AL 3 could belong to the disc component, with a non-negligible probability ($\sim 12\%$).

In Fig. 12, we show histograms relating to the number of probable orbits as a function of pericentric distance (r_{min}), apocentric distance (r_{max}), maximum height above the plane ($|Z|_{\text{max}}$), and eccentricity. If a distance of 6.5 kpc is adopted, then it is clear that AL 3 is a very central cluster, with a maximum height reaching at most $Z \sim 1.5$ kpc, and with a high eccentricity orbit.

Table 3. AL 3: coordinates, magnitudes, and colours of sample stars.

Star	2MASS	α (J2000)	δ (J2000)	V	I	J	H 2MASS	K	J	H VVV	K
B11	18101902-3144506	18 10 19.01	-31 44 50.64	15.902	14.275	13.136	12.440	12.280	13.017	12.397	12.248
B64	18101803-3145435	18 10 18.03	-31 45 43.55	15.703	14.180	13.064	12.456	12.277	13.055	12.529	12.384
B73	18102150-3145268	18 10 21.50	-31 45 26.77	15.709	14.187	13.128	12.449	12.316	13.047	13.047	12.313
F42	—	18 10 17.65	-31 45 38.93	16.054	14.442	—	—	—	—	—	—
F97	18101520-3146014	18 10 15.21	-31 46 00.67	16.037	14.467	13.183	12.481	12.338	—	12.503	12.378
HP1-2	17310585-2958354	17 31 05.60	-29 58 34.00	16.982	14.332	12.210	11.268	10.969	14.588	13.675	13.368
HP1-4	17310538-2959199	17 31 05.30	-29 59 20.00	17.070	14.281	—	11.67	—	11.258	11.392	10.688
HP1-5	17310729-2959021	17 31 07.20	-29 59 02.00	17.131	14.395	11.901	10.869	10.595	12.021	11.285	10.898
AL3-3	18140691-2839087	18 14 06.90	-28 38 09.0	14.524	13.204	12.214	11.631	11.469	12.211	11.714	11.544
AL3-6	18140592-2838049	18 14 05.80	-28 38 06.0	15.563	14.203	12.763	12.272	12.256	—	—	—
AL3-7	18140529-2838168	18 14 05.30	-28 38 19.0	14.313	12.963	11.878	11.296	11.170	11.920	11.472	11.195

Table 4. Adopted stellar parameters for individual stars in NGC 6558, AL 3, and HP 1, and resulting C, N, O abundances. For NGC 6558, the stellar parameters are from Barbuy et al. (2007), and for HP 1 they are from Barbuy et al. (2016). Stellar parameters for the Sun, Arcturus, and μ Leo are also included.

Name	T_{eff} (K)	$\log g$	[Fe/H]	v_t km/s	[C/Fe]	[N/Fe]	[O/Fe]
Program stars							
F42	3800	0.5	-1.05	1.65	-0.5	+0.8	+0.5
HP1-5	4525	2.0	-1.07	1.55	-0.1	0.8	0.5
AL3-3	4250	1.7	-1.00	1.2	-0.1	0.0	0.0
AL3-6	4150	1.3	-1.00	1.2	+0.8	+1.0	+0.8
AL3-7	4500	1.5	-1.00	1.2	-0.2	-0.1	0.0
Reference stars							
Sun	5770	4.44	+0.00	1.0	+0.00	+0.00	+0.00
Arcturus	4275	1.55	-0.54	1.65	+0.11	+0.40	+0.43
μ Leo	4540	2.3	+0.30	1.3	-0.1	+0.65	+0.00

This is typical of the very old, moderately metal-poor globular clusters of the Galactic bulge, similar to NGC 6522, NGC 6558, and HP 1.

On the other hand, if a distance of 6.0 kpc is adopted, according to Ortolani et al. (2006), the cluster reaches distances farther from the Galactic centre with lower eccentricities (see left and bottom and top panels of Figures 11 and 12, respectively). The probabilities also change to an $\sim 60\%$ probability of belonging to the bulge and $\sim 40\%$ to the disc. With this distance, the probability of being part of the disc increases significantly, and maybe this result could be more consistent with the solar CNO abundances.

7. Conclusions

We analysed spectra of individual stars of the globular clusters AL 3, NGC 6558, and HP 1, obtained with the PHOENIX spectrograph at the Gemini South telescope. With a high spectral resolution of $R \sim 75,000$, in the H band centred at 15555 \AA , the wavelength coverage is short ($15520 - 15590 \text{ \AA}$).

In AL 3, this limited wavelength range means that it is difficult to use atomic lines to deduce the stellar parameters effective temperature, gravity, and metallicity. For this reason, we

obtained the effective temperature from the Hydrogen Brackett 16 line, gravity from photometric data, and isochrones. The metallicity $[\text{Fe}/\text{H}] \sim -1.3 \pm 0.3$ was deduced from the observed CMD given in Ortolani et al. (2006) and is confirmed in the present work through analysis of the same CMD. We note that we adopted $[\text{Fe}/\text{H}] = -1.0$ for the analysed stars, due to spectroscopic evidence. For NGC 6558 and HP 1, the stellar parameters were adopted from previous analyses from optical spectra (Barbuy et al. 2007, 2018), and Barbuy et al. (2006, 2016) respectively. Adopting these stellar parameters, we computed the synthetic spectra in order to derive the abundances of C, N, and O. Since they vary interdependently, the fit was done iteratively, where particular attention was given to the CO bandhead. The stars analysed in NGC 6558 and HP 1 show typical CNO abundances of red giants, and confirm previous oxygen abundance derivation.

AL 3 is a more complex case: two stars analysed in AL 3 show solar CNO abundance ratios, but based on very shallow lines, and the location of these two stars in the CMD point to them being AGB stars. The star AL3-6 shows instead very strong CNO abundances of the order of $[\text{C}/\text{Fe}] = +0.8$, $[\text{N}/\text{Fe}] = +1.0$, $[\text{O}/\text{Fe}] = +0.8$. A strong CNO abundance indicated by this cooler star shows that AL 3 appears to be an extremely interesting old cluster. In conclusion, further investigation of this cluster are clearly needed. We also derived the cluster's radial velocity, which in turn allowed us to compute the cluster orbits. For the two AGB stars, we found a higher velocity, whereas for the third cooler star, the radial velocity is compatible with the value from Baumgardt et al. (2019).

The orbital behaviour of AL 3 indicates that it is a typical inner bulge, moderately metal-poor globular cluster if its distance to the Sun is 6.5 kpc (Baumgardt 2019), but if the distance is 6.0 kpc (Ortolani et al. 2006 and present work), there is an increased probability of AL 3 belonging to a disc component. We derive a very old age for AL 3 of 13.4 Gyr, which would point towards an old bulge cluster. Therefore, we conclude that the cluster AL 3 appears to be an extremely interesting cluster that should be further investigated through more wavelength-extended spectra, and including larger samples of member stars.

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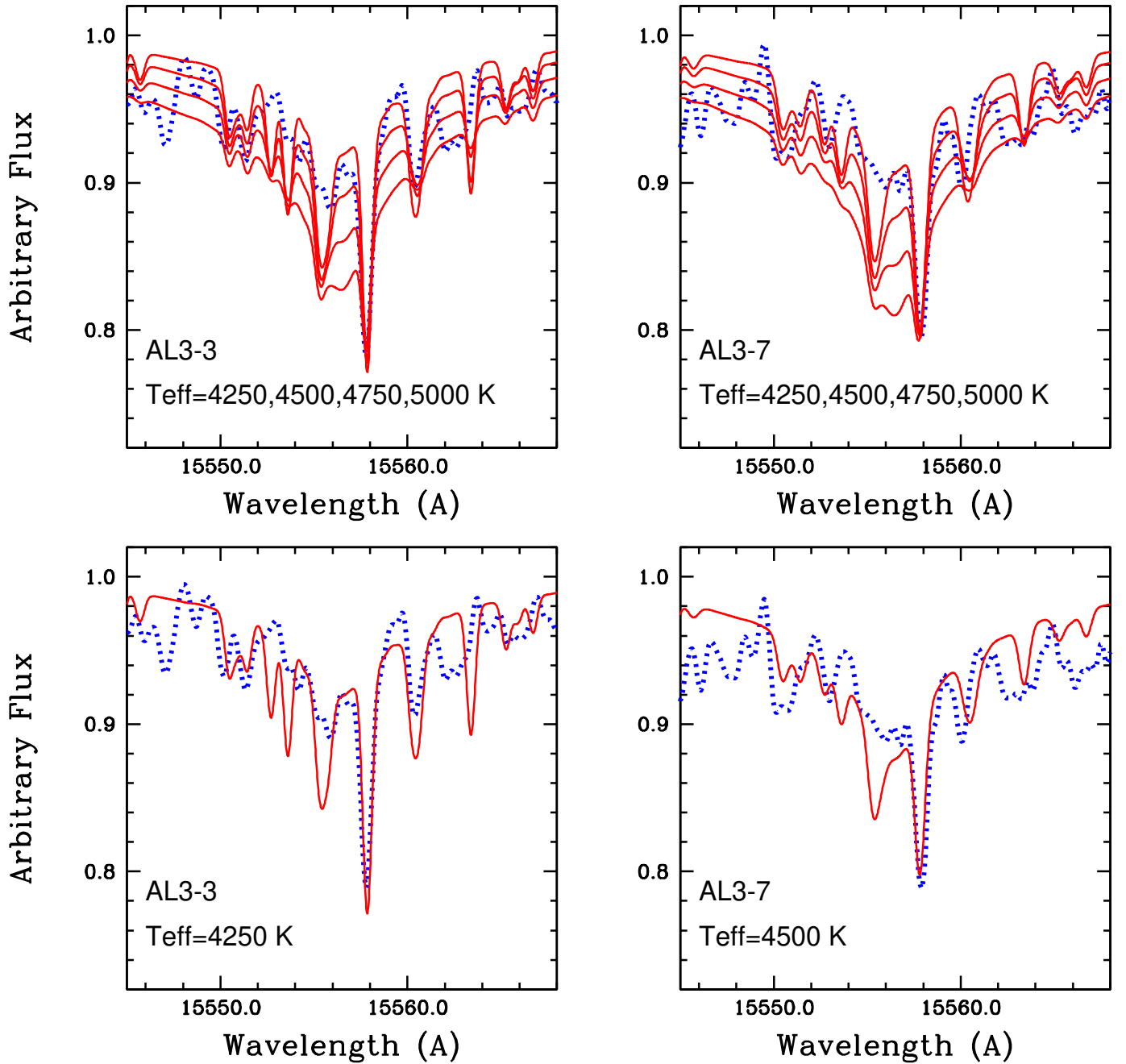


Fig. 6. AL 3-3 and AL 3-7: Hydrogen Brackett 16 line computed for $T_{eff} = 4250, 4500, 4750, 5000$ K (upper panels) and adopted values of 4250 K and 4750 K, respectively (lower panels). The dashed line is the observed spectrum

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References

- Alonso, A., Arribas, S., Martínez-Roger, C. 1998, A&AS, 131, 209
 Alonso, A., Arribas, S., Martínez-Roger, C. 1999, A&AS, 140, 261 (AAM99)
 Andrews, A.D., Lindsay, E.M. 1967, IrAJ, 8, 126
 Barbuy, B., Zoccali, M., Ortolani, S. et al. 2006, A&A, 449, 349
 Barbuy, B., Zoccali, M., Ortolani, S. et al. 2007, AJ, 134, 1613
 Barbuy, B., Chiappini, C., Cantelli, E. 2014, A&A, 570, A76
 Barbuy, B., Friaça, A.C.S., da Silveira, C.R. et al. 2015, A&A, 580, A40
 Barbuy, B., Cantelli, E., Vemado, A. et al. 2016, A&A, 591, A53
 Barbuy, B., Chiappini, C., Gerhard, O. 2018a, ARA&A, 56, 223
 Barbuy, B., Trevisan, J., de Almeida, A. 2018b, PASA, 35, 46
 Barbuy, B., Muniz, L., Ortolani, S. et al. 2018c, A&A, 619, A178
 Bessell, M.S. 1979, PASP, 91, 589
 Bica, E., Ortolani, S., Barbuy, B. 2016, PASA, 33, 28
 Blanco, V.M. 1988, AJ, 95, 1400
 Bland-Hawthorn, J., & Gerhard, O. 2016, ARA&A, 54, 529
 Bressan, A., Marigo, P., Girardi, L. 2012, MNRAS, 427, 127

Table 5. Median orbital parameters and membership probability of AL 3.

Ω_b (km s ⁻¹ kpc ⁻¹)	$\langle r_{\min} \rangle$ (kpc)	$\langle r_{\max} \rangle$ (kpc)	$\langle z _{\max} \rangle$ (kpc)	$\langle e \rangle$	$\mathcal{P}_{\text{bulge}}$ (%)	$\mathcal{P}_{\text{disc}}$ (%)
$d_{\odot} = 6.0$ kpc						
40	1.00 ^{+0.43} _{-0.61}	3.94 ^{+0.52} _{-0.66}	1.36 ^{+0.19} _{-0.15}	0.60 ^{+0.20} _{-0.10}	61.7	38.3
45	0.84 ^{+0.47} _{-0.45}	3.97 ^{+0.55} _{-0.65}	1.36 ^{+0.16} _{-0.13}	0.66 ^{+0.14} _{-0.15}	60.1	39.9
50	0.75 ^{+0.89} _{-0.34}	3.98 ^{+0.72} _{-0.65}	1.31 ^{+0.15} _{-0.10}	0.68 ^{+0.12} _{-0.20}	60.6	39.4
$d_{\odot} = 6.5$ kpc						
40	0.46 ^{+0.69} _{-0.36}	3.34 ^{+0.69} _{-0.61}	1.41 ^{+0.21} _{-0.19}	0.75 ^{+0.18} _{-0.19}	89.2	10.8
45	0.47 ^{+0.50} _{-0.36}	3.39 ^{+0.76} _{-0.67}	1.40 ^{+0.17} _{-0.17}	0.76 ^{+0.17} _{-0.15}	87.9	12.1
50	0.53 ^{+0.35} _{-0.40}	3.42 ^{+0.75} _{-0.73}	1.33 ^{+0.15} _{-0.17}	0.74 ^{+0.17} _{-0.12}	88.5	11.5

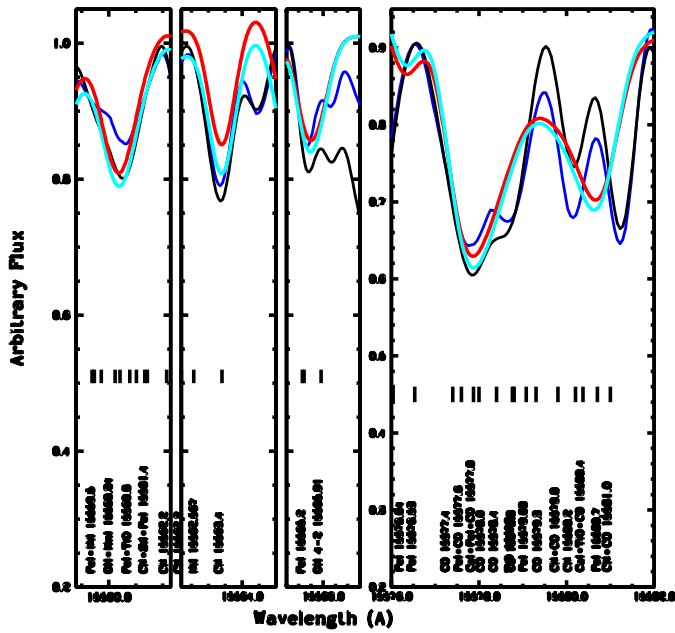


Fig. 7. AL 3-6: Tentative fit to this low S/N spectrum, showing that it is compatible with a high CNO abundance. Blue and black lines: Same observed spectrum normalized in two different ways. Red and cyan lines: Synthetic spectra computed with $[C/Fe]=0.7$ (red), 0.8 (cyan), $[N/Fe]=+1.0$, $[O/Fe]=+0.8$.

Carpenter, J.M. 2001, *AJ*, 121, 2851
 Dias, B., Barbuy, B., Saviane, I. et al. 2015, *A&A*, 573, A13
 Dias, B., Barbuy, B., Saviane, I. et al. 2016, *A&A*, 590, A9
 Dotter, A., Chaboyer, B., Jevremović, D. et al. 2008, *ApJS*, 178, 89
 Dufay, J., Berthier, P., Morignat, B. 1954, *Publ. of the OHP*, 3, No. 17
 Gratton, R.G., Sneden, C. 1990, *A&A*, 234, 366
 Gravity Collaboration, Abuter, R., Amorim, A., et al. 2019, *A&A*, 625, L10
 Grevesse, N. & Sauval, J.N. 1998, *SSRv*, 35, 161
 Grevesse, N., Noels, A., Sauval, J. 1996, *ASP*, 99, p.117
 Grevesse, N., Scott, P., Asplund, M., Sauval, A.J. 2015, *A&A*, 573, 25
 Goldman, A., Schoenfeld, W.G., Goorvitch, D. et al. 1998, *JQSR*, 59, 453
 Goorvitch, D. 1994, *ApJS*, 95, 535
 Gustafsson, B., Edvardsson, B., Eriksson, K., Jørgensen, U. G., Nordlund, Å., Plez, B. 2008, *A&A*, 486, 951
 Harris, W.E. 1996, *AJ*, 112, 1487
 Hinkle, K., Wallace, L., Livingston, W. 1995, *PASP*, 107, 1042
 Huber, K.P., Herzberg, G. 1979, *Constants of diatomic molecules*, Springer, Boston, MA.
 Jørgensen, U.G. 1994, *A&A*, 284, 179
 Kurucz, R. 1993, CD-ROM 23
 Lauberts, A. 1982, *ESO/Uppsala Survey of ESO(B) Atlas*, ESO, Garching
 Lecureur, A., Hill, V., Zoccali, M., et al. 2007, *A&A*, 465, 799

Livingston, W., Wallace, L. 1991, *An atlas of the solar spectrum in the infrared from 1850 to 9000 cm⁻¹ (1.1 to 6.5 micrometer)*, NSO Technical Report, NOAO, Tucson
 Lodders, K., Palme, H., Gail, H.-P. 2009, *Landolt-Börnstein - Group VI Astronomy and Astrophysics Numerical Data and Functional Relationships in Science and Technology Volume 4B: Solar System*. Edited by J.E. Trümper, 2009, 4.4., 44
 Majewski, S.R., Schiavon, R.P., Frinchaboy, P.M. 2017, *AJ*, 154, 94
 Martin, W.C., Fuhr, J.R., Kelleher, D.E., et al. 2002, *NIST Atomic Database (version 2.0)*, <http://physics.nist.gov/asd>. National Institute of Standards and Technology, Gaithersburg, MD.
 McWilliam, A., Wallerstein, G., Mottini, M. 2013, 778, 149
 Meléndez, J., Barbuy, B. 1999, *ApJS*, 124, 527
 Meléndez, J., Barbuy, B., Spite, F. 2001, *ApJ*, 556, 858
 Meléndez, J., Barbuy, B. 2002, *ApJ*, 575, 474
 Meléndez, J., Barbuy, B., Bica, E. et al. 2003, *A&A*, 411, 417
 Navarro, J. F., Frenk, C. S., & White, S. D. M. 1997, *ApJ*, 490, 493
 Ortolani, S., Bica, E., Barbuy, B. 1997, *MNRAS*, 284, 692
 Ortolani, S., Bica, E., Barbuy, B. 2006, *ApJ*, 646, L115
 Pérez-Villegas, A., Rossi, L., Ortolani, S., et al. 2018, *PASA*, 35, 21
 Pérez-Villegas, A., Barbuy, B., Kerber, L. et al. 2020, *MNRAS*, 491, 3251
 Pietrinferni, A., Cassisi, S., Salaris, M., Castelli, F. 2006, *ApJ*, 642, 797
 Piskunov, N., Kupka, F., Ryabchikova, T., Weiss, W., Jeffery, C., 1995, *A&AS*, 112, 525
 Ramírez, I., Allende Prieto, C. 2011, *ApJ*, 743, 136
 Ryabchikova, T., Piskunov, N., Kurucz, R.L. et al. 2015, *PhysS*, 90, 054005
 Rich, R.M., Ortolani, S., Bica, E., Barbuy, B. 1998, *AJ*, 116, 1295
 Rossi, L., Ortolani, S., Bica, E., Barbuy, B., Bonfanti, A. 2015, *MNRAS*, 450, 3270
 Rossi, L. J. 2015, *Astronomy and Computing*, 12, 11
 Saito, R. et al. (VVV collaboration) 2012, *A&A*, 537, 107
 Schiavon, R.P., Barbuy, B. 1999, *ApJ*, 510, 934
 Schönrich, R., Binney, J., & Dehnen, W. 2010, *MNRAS*, 403, 1829
 Souza, S.O., Kerber, L.O., Barbuy, B. et al. 2020, *ApJ*, 890, 38
 Scott, P., Grevesse, N., Asplund, M. et al. 2015a, *A&A*, 573, 26
 Scott, P., Asplund, M., Grevesse, N. et al. 2015b, *A&A*, 573, 27
 Shetrone, M., Bizyaev, D., Lawler, J.E. et al. 2015, *ApJS*, 221, 24
 Skrutskie, M.F., Cutri, R.M., Stiening, R. et al. 2006, *AJ*, 131, 1163
 Smith & Ruck 2000, *A&A*, 356, 570S
 Smith, V. Cunha, K., Shetrone, M.D., et al. 2013, *ApJ*, 765, 16
 Smith, R., Flynn, C., Candler, G. N., Fellhauer, M., & Gibson, B. K. 2015, *MNRAS*, 448, 2934
 Soto, M., Barbá, R., Gunthardt, G., Minniti, D., Lucas, P. et al. 2013, *A&A*, 552, A101
 Steffen, M., Prakashavicius, D., Caffau, E. et al. 2015, *A&A*, 583, A57
 van den Bergh, S., Hagen, G.L. 1975, *AJ*, 80, 11

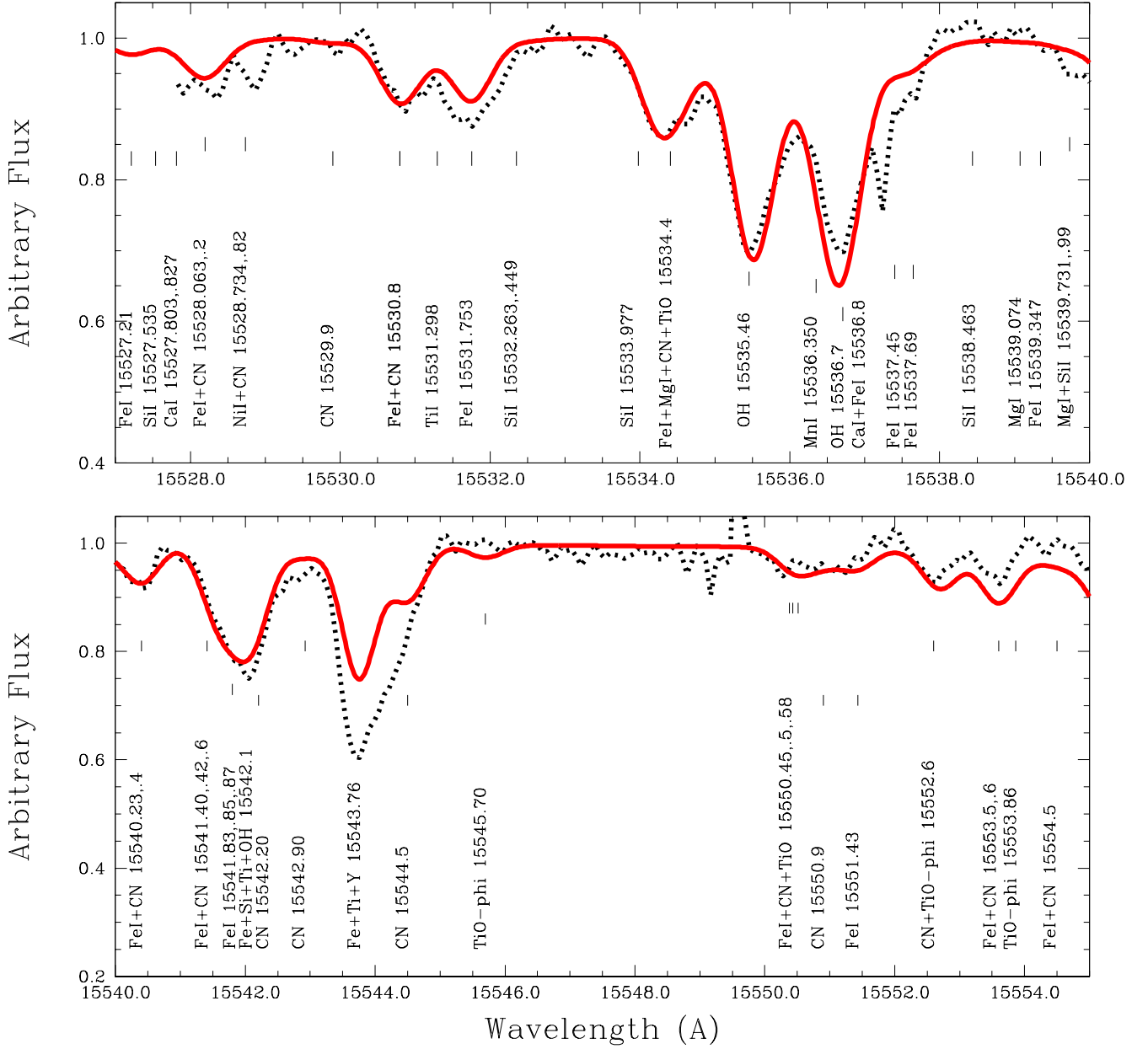


Fig. 8. NGC 6558-42: Line identification in the range 15527-15555 Å. Dashed line: Observed spectrum. Solid red line: Synthetic spectrum. Synthetic spectrum computed with $[C/Fe]=-0.5$, $[N/Fe]=0.8$, $[O/Fe]=+0.5$.

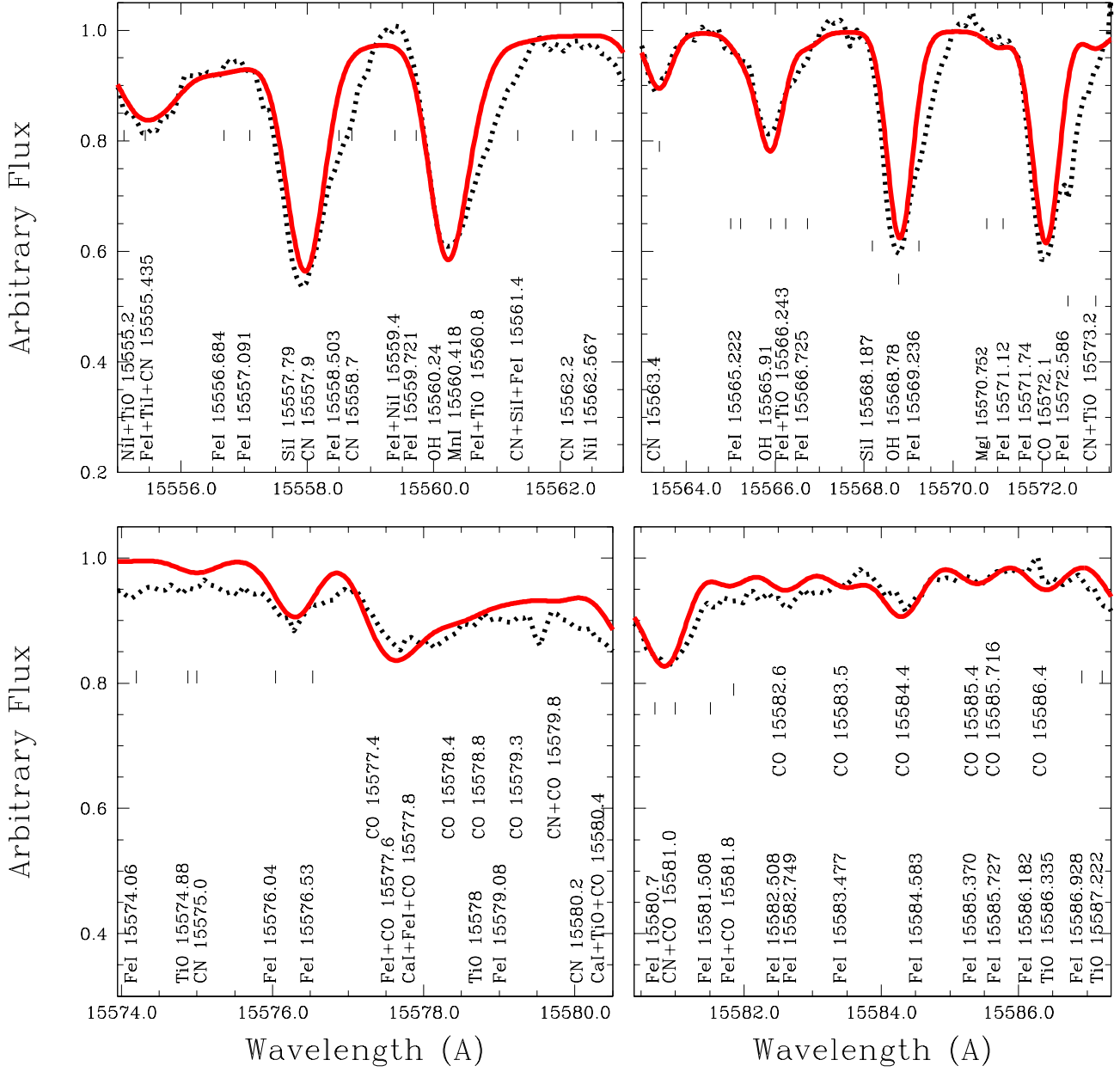


Fig. 9. NGC 6558-42: Same as Fig. 8, in the range 15555-15587 Å.

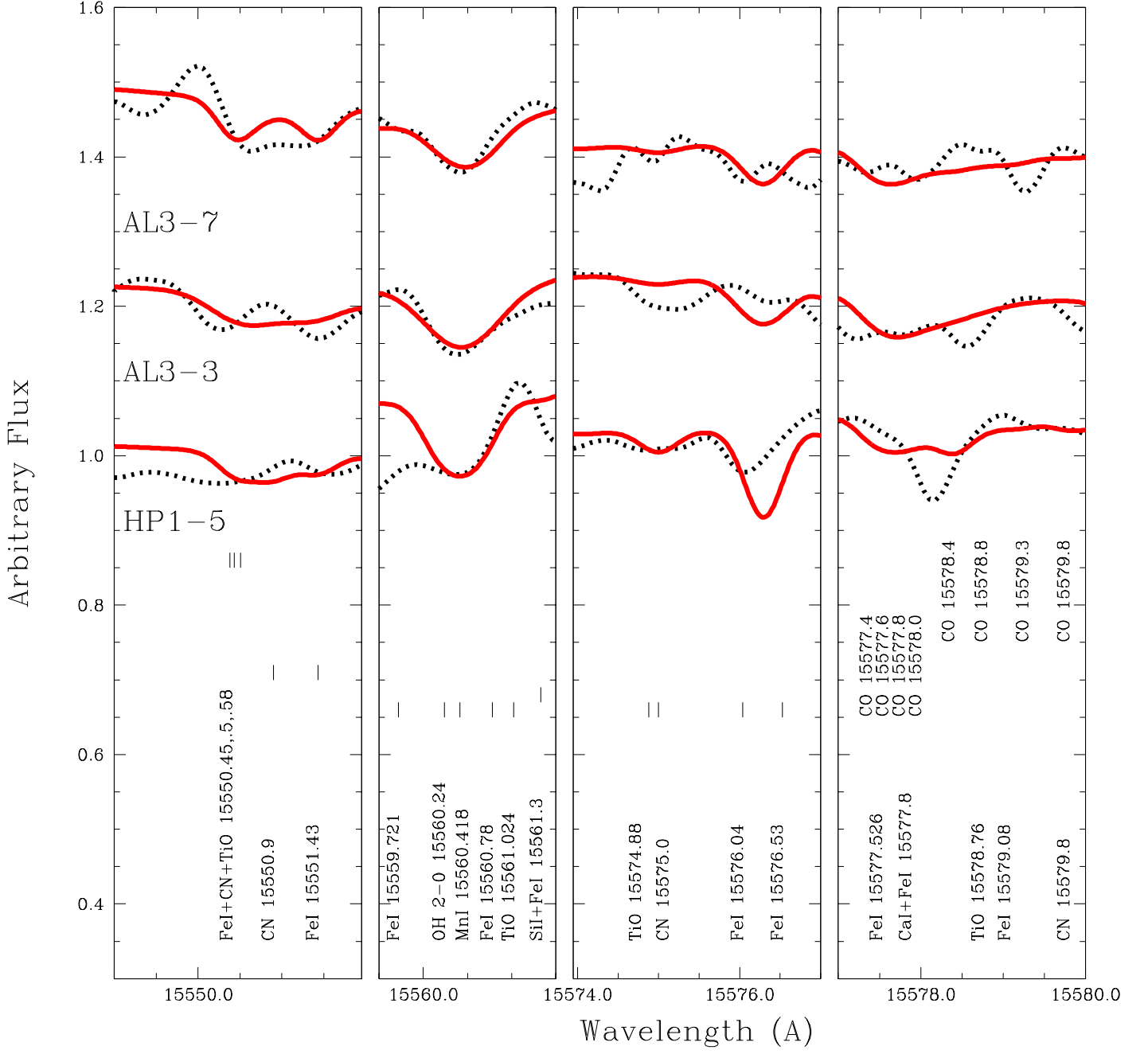


Fig. 10. HP 1-5, AL 3-3, and AL 3-7: Spectrum in selected wavelength regions containing CN, OH lines and the CO bandhead. Synthetic spectra are computed for the CNO abundances given in Table 4.

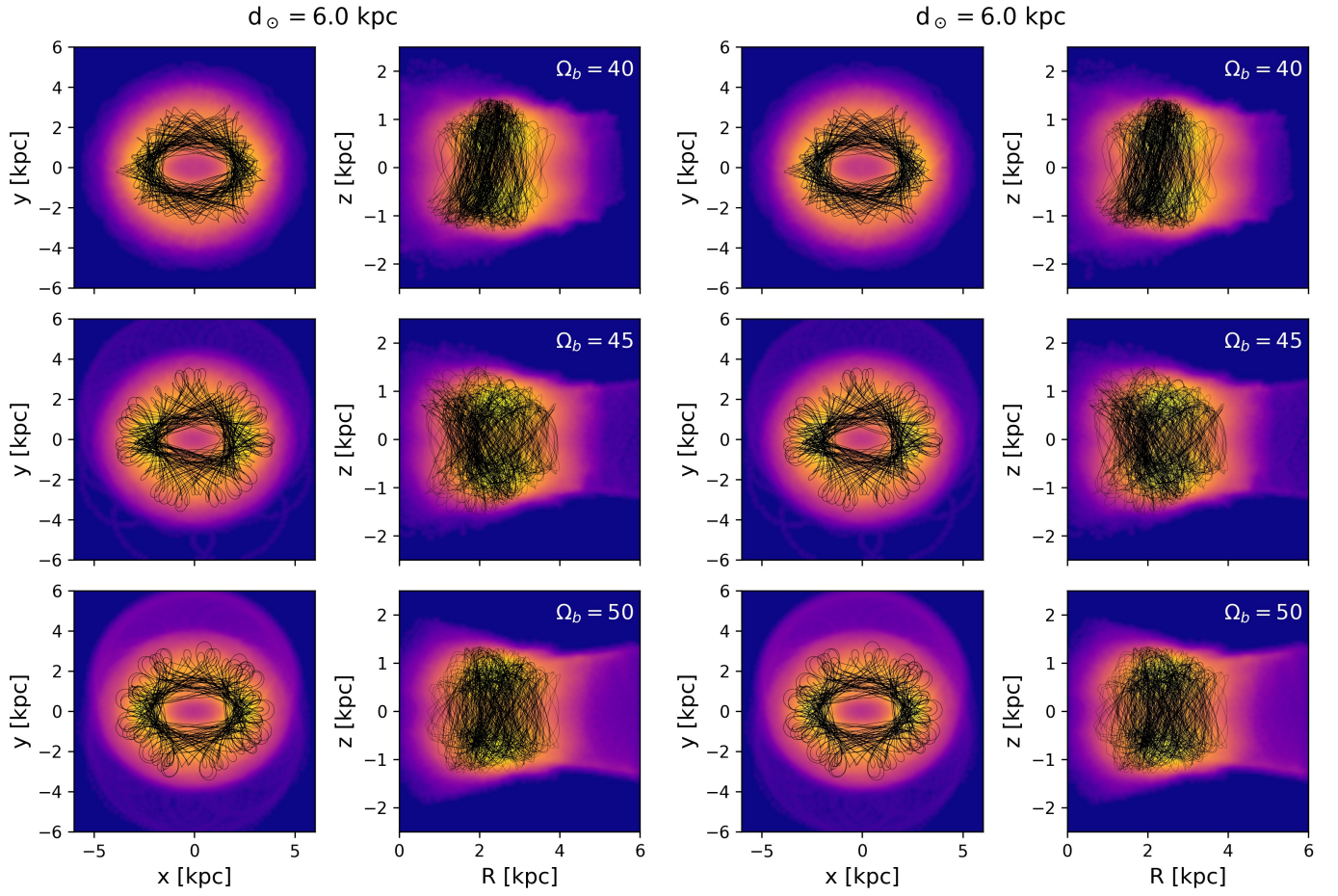


Fig. 11. Probability density map for $x-y$ and $R-z$ projections of the set of orbits for AL 3 for distances of 6.0 kpc (left panels) and 6.5 kpc (right panels), using three different values of $\Omega_b = 40, 45,$ and $50 \text{ km s}^{-1} \text{kpc}^{-1}$. The orbits are co-rotating with the bar frame. Yellow corresponds to the larger probabilities. The black lines show the orbits using the central values.

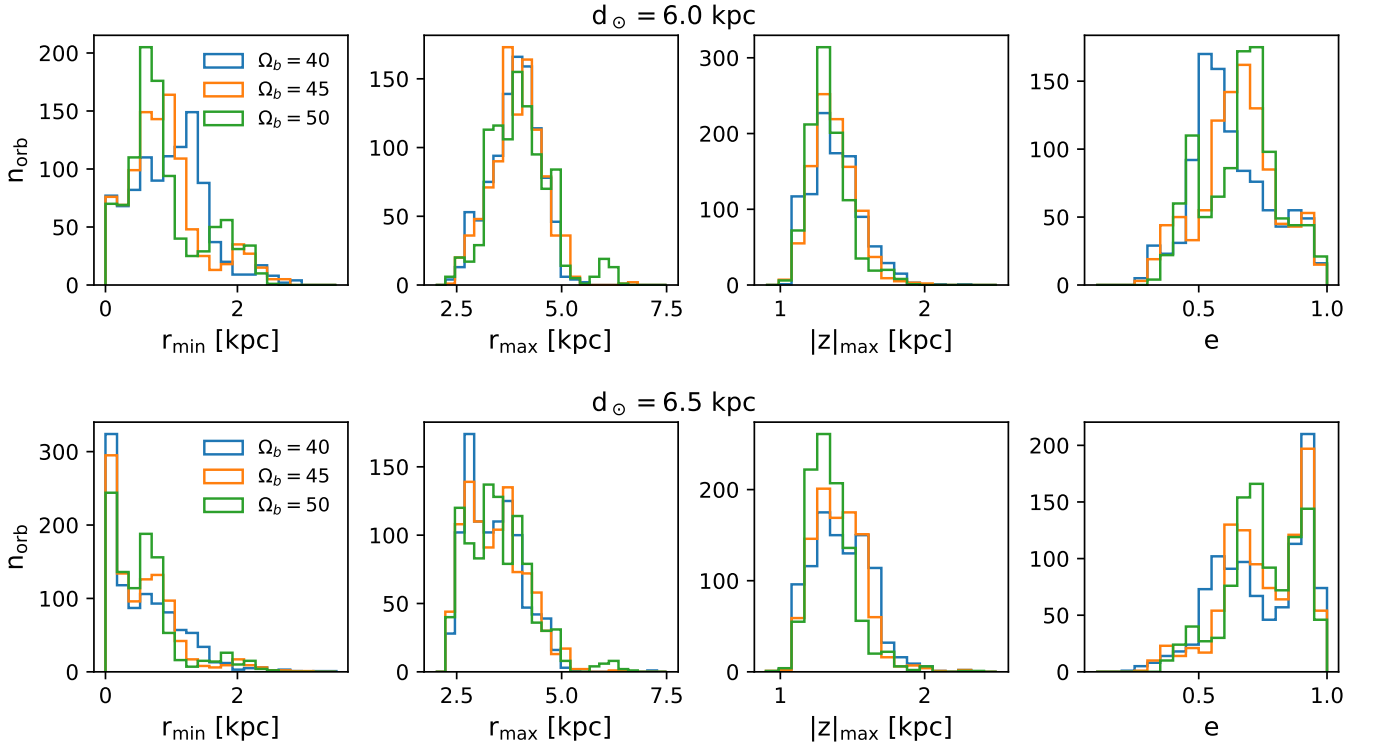


Fig. 12. Distribution of orbital parameters for AL 3, for distances of 6.0 kpc (top panels) and 6.5 kpc (bottom panels), with pericentric distance r_{\min} , apocentric distance r_{\max} , maximum vertical excursion from the Galactic plane $|z|_{\max}$, and eccentricity e . The colours show the different pattern speed of the bar, $\Omega_b = 40$ (blue), 45 (orange), and 50 (green) km s⁻¹ kpc⁻¹.

Appendix A: Isochrone fitting - corner plot

parameter, we adopt the region of highest density as the central value and the uncertainties calculated from the 16th and 84th percentiles.

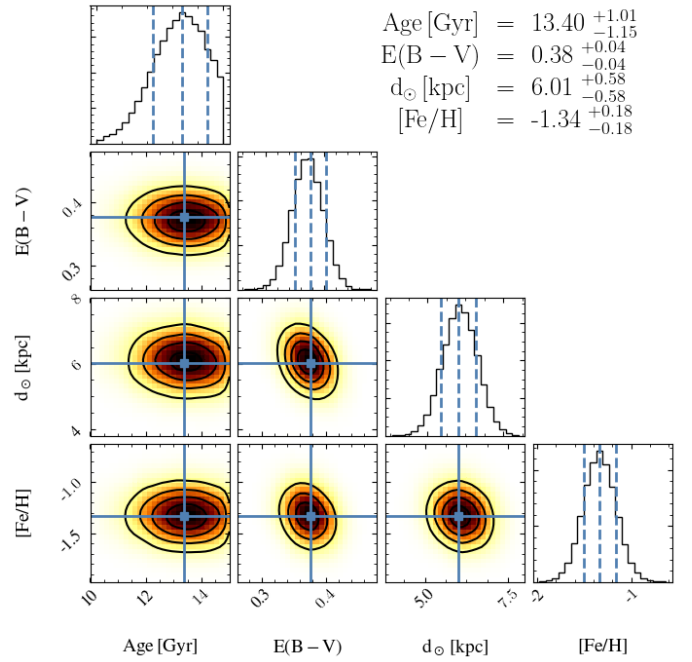


Fig. A.1. Corner plots representing the 4D parameter space of the Markov chain constructed through the Monte Carlo algorithm for the isochrone fitting. To represent the solutions, we adopt the peak of the distribution as the best value, and the uncertainties are computed using the 16th and 84th percentiles. More details are available in Souza et al. (2020).

The SIRIUS code performs the isochrone fitting through the construction of the Markov chain Monte Carlo (MCMC) algorithms. The purpose of the MCMC method is to obtain the posterior distribution of each parameter via the generation of random samples. Figure A.1 shows the corner plots, that is, a graphical representation of the 4D parameter space of the isochrone fitting (age, reddening, distance, and metallicity). The histograms represent the cumulative best solutions (posterior distribution) for each parameter, while the 2D density maps show the correlations between the parameters as well as the region with the highest density. To represent the posterior distributions of each pa-